NMR Detection of pH-Dependent Histidine–Water Proton Exchange Reveals the Conduction Mechanism of a Transmembrane Proton Channel

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Supporting Information

ABSTRACT: The acid-activated proton channel formed by the influenza M2 protein is important for the life cycle of the virus. A single histidine, His37, in the M2 transmembrane domain (M2TM) is responsible for pH activation and proton selectivity of the channel. Recent studies suggested three models for how His37 mediates proton transport: a shuttle mechanism involving His37 protonation and deprotonation, a H-bonded imidazole–imidazolium dimer model, and a transporter model involving large protein conformational changes in synchrony with proton conduction. Using magic-angle-spinning (MAS) solid-state NMR spectroscopy, we examined the proton exchange and backbone conformational dynamics of M2TM in a virus-envelope-mimetic membrane. At physiological temperature and pH, 15N NMR spectra show fast exchange of the imidazole 15N between protonated and unprotonated states. To quantify the proton exchange rates, we measured the 15N T2 relaxation times and simulated them for chemical-shift exchange and fluctuating N–H dipolar fields under 1H decoupling and MAS. The exchange rate is 4.5 × 105 s⁻¹ for N01 and 1.0 × 104 s⁻¹ for Nε2, which are approximately synchronized with the recently reported imidazole reorientation. Binding of the antiviral drug amantadine suppressed both proton exchange and ring motion, thus interfering with the proton transfer mechanism. By measuring the relative concentrations of neutral and cationic His as a function of pH, we determined the four pKₐ values of the His37 tetrad in the viral membrane. Fitting the proton current curve using the charge-state populations from these pKₐ’s, we obtained the relative conductance of the five charge states, which showed that the +3 channel has the highest time-averaged unitary conductance. At physiologically relevant pH, 2D correlation spectra indicated that the neutral and cationic histidines do not have close contacts, ruling out the H-bonded dimer model. Moreover, a narrowly distributed nonideal helical structure coexists with a broadly distributed ideal helical conformation without interchange on the sub-10 ms time scale, thus excluding the transporter model in the viral membrane. These data support the shuttle mechanism of proton conduction, whose essential steps involve His–water proton exchange facilitated by imidazole ring reorientations.

INTRODUCTION

The M2 protein of the influenza virus forms a proton-selective tetrameric channel that allows virus entry into host cells and prevents premature conformational changes of hemagglutinin by maintaining the high pH of the trans-Golgi network.1,2 M2 also mediates membrane scission and virus budding from the host cell.3,4 During virus entry, M2 is activated by the low pH of the endosome and conducts 103–104 protons per second into the virion,5,6 which causes uncoating and release of the ribonucleoprotein into the host cell. A single residue, His37, in the transmembrane domain (TM) (Figure 1a) is responsible for pH activation and proton selectivity of the channel.7,8 The channel is irreversibly inhibited by the antiviral drugs amantadine (Amt) and rimantadine,9 which bind specifically to the TM pore.10–13 The high-resolution structure of the M2 transmembrane domain (M2TM) has been extensively studied by solid-state NMR (SSNMR) spectroscopy,10,14,15 X-ray crystallography,11,16 and solution NMR spectroscopy17 under a range of pH and drug-binding conditions.

Two general mechanisms of proton conduction have been proposed for M2. The water wire model posits that protons are conducted solely by the Grotthuss mechanism18 via a continuous column of H-bonded water molecules when electrostatic repulsion of several cationic His37’s removes the pore constriction at this site (Figure 1b).19–21 His37 plays a passive role in this model and is not directly involved in the proton transfer. A second model posits that protons bind and unbind His37 with every conduction event, causing His37 conformational changes in the process (Figure 1c).22 This “shuttle” model was proposed to explain the measured deuterium isotope effect, pH dependence of the proton current, and saturation conductance of the channel.6,22 We recently reported low-pH specific His37 side-chain reorientation,23 whose minimum energy barrier of 60 kJ/mol is consistent with the proton conduction barrier of ~100 kJ/mol obtained from functional assays,9 supporting the shuttle model.

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On the other hand, the energy barrier for purely water-mediated proton transport in M2 was calculated to be less than 42 kJ/mol, suggesting that protons are not solely conducted by a water wire. These results suggest that His37 shuttles protons into the virion by imidazole protonation and deprotonation facilitated by ring reorientation.

Concurrently, two other His-based proton conduction models were also proposed. The H-bonded dimer model, developed on the basis of molecular dynamics (MD) simulations of the His37 structure and interaction with Trp41, suggests a low-barrier H-bond between NO1 of a neutral His and Ne2H of a cationic His in the +2 tetrad (Figure 1d). The third protonation event, with a pK of 6.3 based on 15N NMR analysis of DMPC/DMPG-bound M2TM, is hypothesized to disrupt this imidazole–imidazolium dimer and establish cation–π interactions between His37 and Trp41. Subsequent conformational fluctuations are envisioned to break this cation–π interaction, exposing Ne2H to the C-terminal water and causing proton transport. Finally, a transporter model was proposed in which the M2 TM backbone alternates between two or more conformations with different water accessibilities to the exterior and interior of the virus, with the motion being synchronized with proton transport. This model was based on experimental and MD-simulated M2 structures showing pH-dependent changes of the tilt angles of the N- and C-terminal halves of the TM helix.

Evaluating these proton conduction models is important not only for influenza virology but also for understanding other ion channels such as voltage-gated proton channels. In this study, we investigated the proton exchange of His37 at physiologically relevant pH, temperature, and membrane composition using magic-angle-spinning (MAS) SSNMR spectroscopy. 15N chemical shift spectra show definitively that His37 is protonated and deprotonated at rates of ~10^3 s^-1 without the formation of imidazole–imidazolium dimers. We determined the four acid dissociation constants in the virus-envelope mimetic (VM) membrane, from which the relative conductances of the different charge states of the channel were estimated. These data show that His37–water proton transfer facilitated by imidazole ring reorientation is the essential proton transport mechanism of M2.

**MATERIALS AND METHODS**

**Membrane Sample Preparation.** The TM (residues 22–46, SSDPLVAAHSIGILHILLWILDLR) of the M2 protein of the Udorn strain of the influenza A virus was synthesized (PrimmBiotech, Cambridge, MA) using Fmoc solid-phase protocols and purified to >95% purity. The peptide was uniformly 13C,15N-labeled at Gly34, His37, and Ile39 or Ile42.

A VM membrane mixture containing 1,2-dipalmitoyl-sn-glycerol-3-phosphocholine (DPPC), 1,2-dipalmitoyl-sn-glycerol-3-phosphoethanolamine (DPPE), egg sphingomyelin (SM), and cholesterol (Chol) was prepared at an SM:DPPC:DPPE:Chol molar ratio of 28:21:21:30. The VM mixture resembles the virus-envelope lipid composition and enhances the spectral resolution of M2TM relative to model phosphocholine bilayers. Importantly, the VM membrane mixture also immobilizes the uniaxial diffusion of the four-helix bundle, thus enabling detection of side-chain motions. The solution was dissolved with a stream of nitrogen gas, suspended in cyclohexane, and lyophilized. The dry lipid powder was resuspended in 1 mL of buffer solution of the desired pH, vortexed, and freeze–thawed eight times to create uniform lipid vesicles. M2 TM powder was codissolved with the detergent octyl-β-D-glucoside (OG) in 1 mL of the same buffer at an OG concentration of 20 mg/mL. The pH of the M2TM/OG solution was adjusted with ~100 μL of dilute HCl or NaOH solution to the desired pH. The solution was then mixed with 1 mL of lipid vesicle solution, vortexed for 2 h, and dialyzed with a 3.5 kDa molecular weight cutoff against 1 L of buffer at 4 °C for 3 days to remove the detergent. The protein–lipid precipitant usually appeared after 1 day. The proteoliposome solution was centrifuged at 15000 g and 6°C for 4 h to yield a membrane pellet with a hydration level of ~40 wt %. The final protein-lipid molar ratio was 1:1.5. The pellet was packed into 4 mm MAS rotors for SSNMR experiments.

Membrane samples were prepared at five pH values from 8.5 to 4.5. The pH 8.5 sample was prepared using a Tris buffer (10 mM Tris, 1 mM EDTA, and 0.01 mM NaN3), the pH 7.0 sample was prepared using a phosphate buffer (10 mM Na2HPO4/NaH2PO4, 1 mM EDTA, and 0.01 mM NaN3), the pH 6.0 sample was prepared using a Bis-Tris buffer (10 mM Bis-Tris, 1 mM EDTA, and 0.01 mM NaN3). The pH 5.2
and pH 4.5 samples were prepared using a citrate buffer (10 mM citric acid/sodium citrate, 1 mM EDTA, and 0.01 mM NaN₃). We also prepared two Amt-bound M2TM samples at pH 6.0 and 5.2 by directly titrating 5–7 μL of Amt-containing solution into the NMR rotor to achieve a final drug:tetramer ratio of 4:1. All buffer pH's were measured at ambient temperature, and the pH of the supernatants after centrifugation was checked and verified to be within 0.1 unit of the desired pH.

**Solid-State NMR Spectroscopy.** SSNMR experiments were carried out on Bruker DSX-400 MHz (9.4 T) and AVANCE 600 MHz (14.1 T) spectrometers (Karlsruhe, Germany) using 4 mm triple-resonance MAS probes. Typical radiofrequency (rF) pulse lengths were 5 μs for ¹³C, 6–7 μs for ¹⁵N, and 3.5–4 μs for ¹H. ¹³C chemical shifts were referenced to the α-Gly CO signal at 176.49 ppm on the tetramethylsilane (TMS) scale, and ¹⁵N chemical shifts were referenced to the ¹⁵N signal of N-acetylvaline at 122.0 ppm on the liquid ammonia scale.

One-dimensional (1D) ¹⁵N cross-polarization (CP) MAS spectra were measured using ¹H spin-lock field strengths of ω₁/2π = 50 kHz. Unprotonated nitrogens, whose concentrations at different pH values are important for determining the His₃⁷ pKₐ's, generally have lower CP efficiencies than the protonated nitrogens because of their weak ¹H–¹⁵N dipolar couplings. To maximize the unprotonated ¹⁵N signal, we used a relatively long CP contact time of 3 ms and optimized the Hartman–Hahn condition by using the model compound N-t-Boc-proline, which contains an unprotonated ¹⁵N. While the optimal CP contact time for maximizing the unprotonated ¹⁵N signal is likely longer than 3 ms, longer contact times reduce the protonated ¹⁵N intensity as a result of ¹H T₁ρ relaxation. Thus, 3 ms was chosen as a compromise. For the pKₐ analysis, where quantitative intensity ratios of the NH and N peaks were required, we used neutral His as the model compound to calibrate the scaling factor k between the NH and N intensities.

¹⁵N T₂ relaxation times were measured at 308 K under 7 kHz MAS using a Hahn echo sequence with a 12 μs 180° pulse. The ¹H decoupling field strength was 62.5 kHz during the echo delays for all samples to ensure that the motion was probed on the same time scale.

Two-dimensional (2D) ¹H-driven ¹³C spin diffusion experiments with a DARR mixing time of 40–60 ms were conducted under 7–10 kHz MAS. 2D ¹⁵N–¹³C correlation spectra were measured using a REDOR-based pulse sequence for ¹³C–¹⁵N polarization transfer. The experiments were conducted at 273 or 243 K under 7–10 kHz MAS. A typical ¹³C–¹⁵N recoupling time of 0.6 ms was used to obtain one-bond ¹⁵N–¹³C cross-peaks. 2D ¹⁵N–¹H dipolar chemical shift (DIPSHIFT) correlation experiments were carried out under 3.7, 3.9, and 5 kHz MAS at 308 K. ¹H homonuclear decoupling was achieved using the MREV-8 sequence at 3.7 and 3.9 kHz MAS and the FSLG sequence at 5.0 kHz MAS. The ¹H 90° pulse length in these homonuclear decoupling sequences was 4 μs. The t₁ time-domain data were fit to obtain the apparent ¹³C–¹⁵N dipolar couplings and then divided by the scaling factor of the homonuclear decoupling sequence (0.47 for MREV-8 and 0.577 for FSLG) to obtain the true couplings.

In measurements of dipolar order parameters, both the homonuclear decoupling scaling factor and the rigid-limit coupling have uncertainties that can affect the values of the order parameters. Thus, we measured the product of these two factors using the crystalline model peptide formyl-Met-Leu-Phe (f-MLF). Using the theoretical scaling factors for MREV-8 and FSLG, we obtained apparent rigid-limit values of 22.7 kHz for the Cα–Hα coupling and high order parameters of 0.95–1.0 for the f-MLF backbone. We used these scaling factors and rigid-limit couplings to extract the His₃⁷ order parameters.

**Numerical Simulations of ¹⁵N T₂ Relaxation Under Exchange and ¹H Decoupling.** ¹⁵N T₂ relaxation was simulated using the exchange-matrix formalism, which involves an exchange matrix, a chemical shift matrix, and a dipolar coupling matrix. The 2 × 2 exchange matrix ρ has diagonal elements equal to −k and off-diagonal elements equal to +k, where k = 1/2T₂. The diagonal chemical shift and dipolar coupling matrices have diagonal elements given by eqs 1a and 1b, respectively:

\[
\rho_{CS,n} = \rho_{iso,n} + C_{1,CSA,n} \cos(\omega_1 t + \gamma_n) + C_{2,CSA,n} \cos(2\omega_1 t + 2\gamma_n)
\]

\[
\rho_{NH,n} = C_{1,NH,n} \cos(\omega_1 t + \gamma_n) + C_{2,NH,n} \cos(2\omega_1 t + 2\gamma_n)
\]

In eq 1a, ρ_{iso,n} is the isotropic chemical shift frequency of site n and the coefficients C_{1,CSA,n} and C_{2,CSA,n} are given by

\[
C_{1,CSA,n} = -\frac{\delta_{CSA,n}}{\sqrt{2}} \sin 2\beta
\]

\[
C_{2,CSA,n} = -\frac{\delta_{CSA,n}}{2} \sin^2 \beta
\]

The coefficients C_{1,NH,n} and C_{2,NH,n} in eq 1b are defined similarly in terms of the dipolar coupling constants δ_{NH,n} which include a factor of 2t₁.

Time was incremented in steps of the dipolar-decoupling pulse spacing τ_{p} = (2\nu_1)^{-1}, where ν₁ = γ_B/2π is the radiofrequency field.

Figure 2. ¹⁵N CP-MAS spectra of His₃⁷-labeled M2TM as functions of pH and temperature. Peak assignments for the Ne²-protonated π tautomer (red), Nδ¹-protonated π tautomer (blue), and cationic His (green), whose structures are shown at the top, were obtained from 2D correlation spectra. (a) pH 4.5. (b) pH 5.2. (c) pH 6.0. (d) pH 7.0. (e) pH 8.5. Spectra were measured at 243, 273, and 308 or 303 K. The exchange intensities at pH 5.2 and 6.0 above 273 K should be noted. Asterisks indicate MAS sidebands.
The inversion and refocusing of the isotropic chemical shift evolution by the $\pi$ pulse (i.e., the Hahn echo) was reproduced by inverting the sign of the chemical-shift frequency matrix. Similarly, continuous-wave (CW) dipolar decoupling was approximated by dipolar-frequency inversion by a sequence of 180° pulses spaced by $t_{\pi\pi}$.

$$S(t = 2Nt_{\pi\pi}) = \frac{1}{2} \cdot \frac{T}{\pi} \cdot \prod_{n=1}^{N} e^{[\delta N_{\text{C}}(\sigma_{n\pi}) + (-1)^{n} \delta N_{\text{C}}(\sigma_{n\pi})]/T_{2} + B t_{\pi\pi}},$$

$$\times \prod_{n=1}^{N} e^{[\delta N_{\text{H}}(\sigma_{n\pi}) + (-1)^{n} \delta N_{\text{H}}(\sigma_{n\pi})]/T_{2} + B t_{\pi\pi}} \cdot T$$

(3)

thus giving the same average nutation angle as CW decoupling. To speed up the calculation, the products of exponential matrices were evaluated for one rotation period ($T_{2}$), and the $k^{	ext{th}}$ powers of these product matrices were then used to calculate the signal after $2K$ rotor periods. The $T_{2}$ relaxation time was obtained from the condition $S(T_{2}) = e^{-1} = 0.37$.

The location of the $T_{2}$ minimum and the change in $T_{2}$ with the exchange rate $k$ for purely dipolar modulations under pulsed decoupling were as predicted by Rothwell and Waugh for CW decoupling,$^{37}$ while the depth of the $T_{2}$ minimum agreed within 20%. In the simulations, we increased the dipolar coupling strength by 10% to match the experimentally observed $T_{2}$ relaxation time and was set to zero in eq 1a to simplify the simulations.

With the frequency and exchange matrices in the same exponents in eq 3, changes in chemical shift and dipolar frequencies occur concomitantly, as in reality. Curves for individual processes, including pure chemical exchange, the MAS effect on the chemical shift anisotropy, and pure dipolar modulation under heteronuclear decoupling, were obtained by setting all other coupling constants or shift differences to zero but otherwise retaining MAS and decoupling.

The chemical shift anisotropy (CSA) is contained in $\omega_{\text{CS,eq}}$ in eq 1a. The CSA has been found to have little effect on the overall $T_{2}$ relaxation times. This is expected from the theory of MAS, which refocusses the moderate CSA-induced dephasing of the magnetization within a relatively short time, the rotor period. Similarly, the chemical shift asymmetry parameter $\eta$ has no detectable effect on the total $T_{2}$ relaxation time and was set to zero in eq 1a to simplify the simulations.

The chemical shift change due to deprotonation was approximated as a change of $2\pi \times 2$ kHz (50 ppm) in the CSA parameter $\delta_{\text{CS}}$. For powder averaging, the angle $\beta$ in eqs 2a and 2b was varied in 135° steps.

**RESULTS**

$^{15}$N NMR Spectra Indicate His37 Protonation and Deprotonation at Physiological pH and Temperature. The $^{13}$C and $^{15}$N MAS spectra of His37-labeled M2TM in the mildly acidic pH range 7–5 are shown in Figure 2 and Figure S1 in the Supporting Information and compared with spectra at pH 8.5 and 4.5.$^{13}$ The $^{15}$N chemical shifts are highly sensitive to the protonation state of the imidazole: unprotonated $N_{\text{oH}}$ in the $\pi$ tautomer and $N_{\text{oH}}$ in the $\pi$ tautomer of neutral His resonate at $\sim$250 ppm, while protonated $^{15}$N in cationic and neutral His resonate at 160–190 ppm. 2D correlation spectra (Figure 3) distinguished the protonated $^{15}$N($\pi$H) (176 ppm) and $N_{\text{oH}}$ (180 ppm) of cationic His from the protonated $^{15}$N($\pi$H) of His at 159 and 170 ppm, respectively. At low temperature, the $^{15}$N spectra (Figure 2, left column) show the expected trend of higher cationic His intensity and lower neutral His intensity with decreasing pH. More importantly, at 303–308 K and between pH 5.2 and 7.0, the $^{15}$N spectra reveal chemical exchange of the imidazole nitrogens. At pH 5.2, the 250 ppm peak present at 243 K disappeared above 273 K and a new 213 ppm peak appeared at 308 K (Figure 2b). This frequency is halfway between the unprotonated (250 ppm) and protonated (178 ppm) $^{15}$N chemical shifts, indicating that it results from equal-population exchange between the two species. Thus, the imidazole rings...
undergo protonation and deprotonation at 308 K at a rate much faster than the 15N chemical shift difference (Δν) of ~70 ppm or ~3000 s⁻¹. The protonation and deprotonation events can be attributed to His-water proton exchange but are inconsistent with His–His H-bonding, as we show below. Between NØ1 and Nr2, the more likely candidate for the 213 ppm exchange peak is NØ1 (Figure 4a) because chemical shift assignment 35 indicates that Nr2 has higher proton affinities than NØ1 in His37. Nr2 is the main protonated nitrogen at high pH (Figure 2c) and preserves its protonated chemical shift (159 ppm) from pH 8.5 to 6 before moving downfield at lower pH. Previous bond length measurements indicated a short Nr2–H bond length of 1.03 Å at pH 8.5, 35 also supporting the high proton affinity of Nr2.

In addition to the 213 ppm exchange peak, we also observed a broad-intensity band from 190 to 220 ppm for pH 7 to 5.2 at high temperature. The broadening could be inhomogeneous as a result of a distribution of neutral to charged His ratios, [His]/[HisH⁺], or homogeneous as a result of exchange at rates comparable to the 15N isotopic chemical shift difference. We measured 15N T² relaxation times to distinguish these two possibilities (Figure S2 in the Supporting Information): at pH 5.2, the broad band has a T² of 1.7 ms, indicating a homogeneous line width of 4.7 ppm, which is much narrower than the 30 ppm span of the broad peak. Thus, most of the line broadening is inhomogeneous in nature. The center of mass of the broad band is closer to the protonated chemical shift than the unprotonated one, suggesting that the equilibrium is shifted to the protonated state. Since Nr2 has a higher proton affinity, we attribute this broad band to Nr2 exchange (Figure 4b).

Not all of the NØ1 and Nr2 participate in exchange: the 308 K spectrum at pH 5.2 shows residual intensities at 173 and 185 ppm, indicating that some nitrogens retain their protons most of the time. We attribute the 173 ppm peak to nonexchanging Nr2H and the 185 ppm peak to nonexchanging NØ1H.

To test whether the 15N exchange peaks result from H-bonding between neutral and cationic His, as proposed in the dimer model 15,24 we measured 2D 13C–13C correlation spectra at pH 6, where both neutral and cationic His are present (Figure 3c) and where most channels are in the +2 state (see below). If strong H-bonded dimers exist, cross-peaks between neutral and charged side chains would be expected. The CÔ2 peak is well-resolved between the neutral tautomer (112 ppm) and cationic imidazolium (118 ppm), thus providing a good probe of intermolecular contacts. The dimer model 15 predicts a CÔ2(τ) to CÔ2(+) distance of 5.9 Å, which is within the distance reach of 13C spin diffusion. Figure 3c and Figure S3 in the Supporting Information show that CÔ2(τ)–CÔ2(+) correlation is absent at mixing times from 40 to 300 ms. In contrast, intertautomer CÔ2(τ)–CÔ2(+) cross-peaks were detected at pH 8.5 within as short a time as 40 ms (Figure 3d), confirming that 13C spin diffusion is able to detect close intermolecular contacts within the His37 tetrad. Thus, the 2D spectra exclude the H-bonded dimer model.

Quantification of Proton Exchange Rates through 15N T² Relaxation under ¹H Decoupling. To quantify the NH–15N exchange rate, we first considered two-site exchange averaging only isotropic chemical shifts. In this scenario, the exchange rate is can be determined from the exchange-induced 15N T² relaxation time (T²') and the isotropic shift difference Δν according to the expression $k = \pi^2 \Delta \nu T^2' / 2$. For the 213 ppm exchange peak at pH 5.2, we measured an 15N T² of 2.8 ms, while the nonexchanging backbone amides have T²'s of ~10 ms (Figure S2 and Table S1 in the Supporting Information). Thus, the exchange-induced T²' is 3.9 ± 0.5 ms. With a chemical shift difference of ~3000 Hz, the rate based on the two-site isotropic-shift exchange model is thus $1.8 \times 10^5$ s⁻¹.

However, for chemical exchange in solids under ¹H dipolar decoupling, we need to consider the fact that exchange-induced fluctuations of the 15N–¹H dipolar coupling interfere with coherent averaging by ¹H decoupling. Similarly, fluctuations of the 15N CSA interfere with time averaging by MAS. We performed numerical simulations to take into account all of these effects quantitatively. An analytical theory for part of this problem, heteronuclear dipolar T² relaxation under ¹H decoupling, has been described by Rothwell and Waugh. 37 However, the theory was derived for nonspinning solids assuming that isotropic rotational diffusion drives the relaxation, not for two-site exchange in a solid under MAS. To modify that theory for our purpose, we start with the following expression for the time-dependent change in the density operator $\rho$ (eq 7 in ref 37):

$$\frac{d\rho}{dt} = -\sum_{n=\pm 1} [S_{I,I_n} [S_{I,I_0}, \rho]] / \int_0^\infty \gamma_I^1 / \gamma_S^1 \beta^2 \left( \frac{\beta(t) - \beta(t-t)\tanh(t)}{\tau(t) - \tau(t-t)} \right) e^{-\beta(t)\tau(t)} dt$$

(4)

where $\gamma_I$ and $\gamma_S$ are the gyromagnetic ratios of the I spin (¹H) and the heteronuclear spin S (¹⁵N), respectively, and $D_{00}(t)$ is a Wigner rotation matrix with an angular dependence $[3 \cos^2 \beta(t) - 1]/2$. In addition to removing the nonsecular terms, we have added an ensemble average over the $D_{00}(t)$ terms and moved...
the distance-dependent term into the integral over \( \tau \) because the internuclear distance \( r \) fluctuates during deprotonation and protonation of the nitrogen. Next, we define a frequency correlation function \( C_\omega(\tau) \) as

\[
C_\omega(\tau) \equiv \langle \omega(t)\omega(t - \tau) \rangle
= \gamma_1^2 \gamma_2^{2K} \langle \frac{D_{\omega,0}(t) D_{\omega,0}^*(t - \tau)}{r^3(t) - r^3(t - \tau)} \rangle
\]  

(5)

The time evolution of the density operator is related to the correlation function as follows:

\[
\frac{d\rho}{dt} = -\sum_{n = \pm 1} [S_n I_n, S_{-1 - n} \rho] \int_0^\infty C_\omega(\tau) e^{-i\omega\tau} d\tau
\]  

(6)

The correlation function decays exponentially toward its asymptotic value \( C_\omega(\infty) \) with a time constant \( \tau_C \):

\[
C_\omega(\tau) = [C_\omega(0) - C_\omega(\infty)] e^{-\tau/\tau_C} + C_\omega(\infty)
\]  

(7)

The constant term in eq 7, \( C_\omega(\infty) \), can be disregarded in the following since it contributes to the spectral density only at \( \omega = 0 \) and not at \( \omega_1 \).

For exchange between two equally populated sites with frequencies \( \omega_A \) and \( \omega_B \), the correlation function at \( \tau = 0 \) is

\[
C_\omega(0) = \langle \omega(t)\omega(t) \rangle = \langle \omega_A^2 + \omega_B^2 \rangle / 2
\]  

(8)

Assuming that the \( N-H \) vectors in sites A and B are parallel, or that \( \omega_B \) is negligibly small, we can factorize \( \langle (\omega_A - \omega_B)^2 \rangle / 4 \) as

\[
\frac{\langle (\omega_A - \omega_B)^2 \rangle}{4} = \frac{(\delta_A - \delta_B)^2}{4} \left\langle \left( \frac{3\cos^2(\beta - 1)}{2} \right)^2 \right\rangle
\]  

\[= \frac{(\delta_A - \delta_B)^2}{4\delta_A^2} \left\langle \left( \frac{3\cos^2(\beta - 1)}{2} \right)^2 \right\rangle
\]  

(9)

where the dipolar coupling constants are \( \delta_A = \gamma_y\gamma_S h / r_A^3 \) and \( \delta_B = \gamma_y\gamma_S h / r_B^3 \) and \( \beta \) is the angle between the \( N-H \) vector and the external field \( B_0 \). Since the term corresponding to eq 9 in the Rothwell—Waugh theory for isotropic rotational diffusion is \( \left\langle \frac{(\delta_A - \delta_B)^2}{4\delta_A^2} \right\rangle \), the prefactor \( \left\langle \frac{(\delta_A - \delta_B)^2}{4\delta_A^2} \right\rangle \) is the only modification to the Rothwell—Waugh equations. This factor carries through to their eq 10, which in the current context reads

\[
\frac{1}{T_2} = \frac{(\delta_A - \delta_B)^2}{4\delta_A^2} \gamma_1^2 \gamma_2^{2K} \frac{1}{5r_A^6} \frac{\tau_C}{1 + \omega_1^2 \tau_C^2}
\]  

(10)

For \( \delta_A = 2\pi \times 10^4 \) Hz for an \( N-H \) bond and \( \delta_B = 2\pi \times 1 \) kHz for an unprotonated \( N \),

\[
\frac{(\delta_A - \delta_B)^2}{4\delta_A^2} = \frac{81}{4 \times 100} = 0.20
\]  

(11)

Thus, the dipolar relaxation rate is 5 times smaller than the value obtained if the original Rothwell—Waugh theory is incorrectly applied to the histidine nitrogen undergoing proton exchange. The 5-fold difference arises essentially because half of the time the nitrogen is not protonated and thus has a weak coupling to protons.

Figure 4c shows the calculated \( ^{15}N \) \( T_2^* \) as a function of the exchange rate \( k_\text{ex} \), where all three effects, isotropic chemical shift exchange, CSA modulation under MAS, and \( N-H \) dipolar modulation under \( ^1H \) decoupling, are considered separately and in combination. The \( T_2^* \) curves for these processes have minima when the exchange rate is half the relevant frequency \( \omega_{ex} \), i.e., the isotropic-shift difference \( 2\pi\Delta\nu \), the MAS frequency \( \omega_{ex} \), and the \( ^1H \) dipolar decoupling field strength \( \omega_{ex} \), as expected for \( \omega_{ex} \tau_C \approx 1 \) and \( k = 1/2\tau_C \). Over a wide range of motional rates, the 3 kHz isotropic-shift exchange is the dominant relaxation mechanism. The effects of the 10 kHz fluctuating \( N-H \) dipolar fields are limited by the sufficiently large (63 kHz) \( ^1H \) decoupling field strength, while the effects of the smaller (~2 kHz) \( ^{15}N \) CSA fluctuations are strongly suppressed by 7 kHz MAS. The global \( T_2^* \) minimum occurs when \( k \) matches the isotropic shift difference, while the \( T_2^* \) contribution from exchange dynamics interfering with \( ^1H \) decoupling is minor because the nitrogen is protonated only about half the time. The effects of MAS are quite negligible, and the total relaxation rate is quite well approximated as the simple sum of the relaxation rates due to chemical shift exchange and dipolar modulation. The measured \( T_2^* \) value of 3.9 ms for the 213 ppm peak translates to a proton exchange rate of \((4.5 \pm 1.0) \times 10^4 \text{ s}^{-1}\). A second solution in the slow regime, ~250 s\(^{-1}\), can be excluded by motional narrowing of the \( ^{15}N \) spectra, which requires an exchange rate much faster than \( 3000 \text{ s}^{-1}\). For the broad exchange band assigned to \( \text{His}2 \), the measured \( T_2^* \) values at pH 5.2 and 6.0 are 0.9~20 ms (Table S1 in the Supporting Information), which correspond to exchange rates of \((1.0 \pm 0.5) \times 10^5 \text{ s}^{-1}\). These \( 10^5 \text{ s}^{-1} \) rates are about an order of magnitude larger than the proton exchange rates of buffered solutions at similar pH. This difference is expected because the diffusion-limited exchange should be facilitated by the confinement of His37 in the small cavity of the channel.

**Proton Dissociation Constants of the His37 Tetrad in M2 Bound to the Virus-Envelope-Mimetic Membrane.** The \( ^{15}N \) NMR spectra not only reveal the kinetics of proton exchange, but also give rich information on the protonation equilibria of the His37 tetrad in the VM membrane. We integrated the protonated and unprotonated \( ^{15}N \) signals at 243 K. The intensity ratios \( I_{\text{NH}_3}/I_{\text{NH}} \) directly indicate the concentration ratio of neutral to cationic histidines as a function of pH, from which the four equilibrium constants can be calculated (eqs S4 and S5 in the Supporting Information). The intensity ratios were measured at five different pH values for four unknown pK\(_a\)s, and thus, the problem was overdetermined. The 243 K \( ^{15}N \) spectra (Figure 2, left column) were used for peak integration because the low-temperature intensities are minimally affected by motional averaging. We assume that the temperature dependence of the histidine pK\(_a\) values can be neglected because it should be largely canceled by the temperature dependence of the buffer pK\(_a\), which has a similar trend and magnitude. Figure 5a plots the \( I_{\text{NH}_3}/I_{\text{NH}} \) ratios as a function of pH, and the corresponding [His]/[His\(^{\text{H}^+}\)] ratios are shown in Figure 5b. Fitting the latter yielded four pK\(_a\)s for the His37 tetrad in the VM-membrane-bound M2TM: 7.6 ± 0.1, 6.8 ± 0.1, 4.9 ± 0.3, and 4.2 ± 0.6 (gray vertical lines), where the error bars include both systematic uncertainties in the sample pH and the propagated random uncertainties in the intensity ratios (Table S2 in the Supporting Information). For comparison, the pK\(_a\)s of the peptide in DMPC/DMPG bilayers have
Figure 5. Protonation equilibria of the His37 tetrad in VM-membrane-bound M2TM. (a) \(I_{NH}/I_0\) without drug (black) and with drug (red). (b) \([\text{His}]/[\text{His}^+]\) ratios (●) as a function of pH and the best-fit curve (solid line), from which the four \(pK_a\)’s were obtained. For comparison, the \([\text{His}]/[\text{His}^+]\) ratios reported previously for DMPC/DMPG-bound M2TM (○ and dashed line)\(^2\) are also shown. (c) Proton currents of Udorn M2 (red ■) and normalized populations of all five charge states (symbols and dotted lines) as a function of pH. The best fit of the proton currents (solid red line) was obtained using relative time-averaged unitary conductances of 1.9 ± 0.2, 5.5 ± 0.7, and 0.4 ± 1.6 for the +2, +3, and +4 channels, respectively, and 0 for the +1 and neutral channels.

been reported\(^2\) as 8.2, 8.2, 6.3 and <5 on the basis of a different set of measured \([\text{His}]/[\text{His}^+]\) values (Figure 5b, dotted line). Therefore, in comparison with the previous model-membrane result, the four histidines are protonated at lower pH and the first two protonation steps are resolved in the cholesterol-rich VM membrane. The methods for extracting \(pK_a\)’s differ between the two studies. We obtained \([\text{His}]/[\text{His}^+]\) ratios from the relative intensities of unprotonated and protonated \(^{15}\text{N}\) signals, which are resolved by more than 70 ppm. The different \(^{1}\text{H}^{15}\text{N}\) CP efficiencies of N and NH signals were taken into account by calibration using a model compound (Figure S4 in the Supporting Information), so the intensity ratio accurately reflects the relative amounts of unprotonated and protonated nitrogens. In comparison, the previous model-membrane study\(^2\) obtained \([\text{His}]/[\text{His}^+]\) ratios by deconvolution of the broad protonated \(^{15}\text{N}\) peak into multiple components, which had large uncertainties due to significant exchange broadening of these peaks at the temperature of the experiments. Apart from experimental uncertainties, the \(pK_a\) differences may also reflect real differences in the protonation equilibria of M2TM in the two lipid membranes: the anionic DMPG used in the previous study may increase the local concentration of protons on the bilayer surface, thus increasing the apparent \(pK_a\) values.

To relate the His \(pK_a\)’s to electrophysiological data, we fit the proton currents of Udorn and Weybridge M2 (Table S3 in the Supporting Information)\(^4\) as the population-weighted sum of the time-averaged unitary currents. We assumed that the equilibrium populations of the four charge states, which are fully determined by the \(pK_a\)’s, were applicable to the kinetic conditions under which the proton currents were measured. The charge-state populations of the channels, \(N_i\), are related to the acid dissociation constants \(K_i\) according to

\[
\begin{align*}
N_{+4} &= \frac{[\text{H}^+]^4}{\Sigma} \\
N_{+3} &= \frac{[\text{H}^+]^3 K_1}{\Sigma} \\
N_{+2} &= \frac{[\text{H}^+]^2 K_1 K_2}{\Sigma} \\
N_{+1} &= \frac{[\text{H}^+] K_1 K_2 K_3}{\Sigma} \\
N_0 &= K_1 K_2 K_3 K_4 / \Sigma
\end{align*}
\]

where the normalization constant is \(\Sigma = [\text{H}^+]^4 + [\text{H}^+]^3 K_1 + [\text{H}^+]^2 K_1 K_2 + [\text{H}^+] K_1 K_2 K_3 + K_1 K_2 K_3 K_4\). Figure 5c plots the populations of the five charge states of the channel as functions of pH. As expected, the more cationic tetrad is populated at lower pH, and the intersections of the population curves of two neighboring charge states correspond to the \(pK_a\)’s (gray vertical lines).

The proton current at a certain pH is the electrochemical potential multiplied by the sum of the products of the population \(N_i\), the open probability \(P_{o,i}\), and the unitary conductance \(g_i\) for each charge state \(i\):

\[
I = (V - E_{\text{H+}}) \sum_{i=0}^{+4} N_i P_{o,i} g_i
\]

The electrochemical potential, which provides the driving force for proton conduction, is the difference between the applied voltage \(V\) and the Nernst potential \(E_{\text{H+}}\). The latter results from the pH difference between the inside and outside of the membrane: \(E_{\text{H+}} = 2.303RT(\text{pH}_{\text{in}} - \text{pH}_{\text{out}})/F\), where \(R\) is the gas constant, \(T\) is the temperature, and \(F\) is the Faraday constant. The product of the unitary conductance and the open probability is the time-averaged single-channel conductance \(\bar{g}_i\):

\[
\bar{g}_i = P_{o,i} g_i
\]

We fit two sets of proton current data. Wang et al.\(^7\) reported proton currents of Udorn M2 using an applied voltage of −120 mV, \(\text{pH}_{\text{in}} = 7.5\), and \(\text{pH}_{\text{out}} = 4.5\). Chizhmakov et al.\(^4\) reported the chord conductance \(g = I/(V - E_{\text{H+}})\) for the Weybridge strain of M2 using an applied voltage of −60 mV, \(\text{pH}_{\text{in}} = 7.4\), and \(\text{pH}_{\text{out}} = 4.0\). (Table S3 in the Supporting Information). The latter data set can be fit using the equation

\[
\frac{g}{g_{\text{max}}} = \sum_{i=0}^{+4} N_i P_{o,i} g_i = \sum_{i=0}^{+4} N_i \bar{g}_i
\]

Figure 5c shows the Udorn M2 proton current data (red squares) as a function of pH. The current reaches a maximum near the lowest pH of 4.5 and is close to zero above neutral pH. Qualitatively, this already indicates that the neutral and +1 tetrad, which are predominantly populated above pH 7, conduct few protons, while the +3 channels, whose population curve has a very similar pH dependence as the functional curve with a maximum near pH 4.5, are chiefly responsible for proton conduction. Qualitative fitting of the proton current curve using the charge-state populations gave relative \(\bar{g}_i\) values of
1.9 \pm 0.2, 5.5 \pm 0.7, and 0.4 \pm 1.6 for the +2, +3, and +4 charge states, respectively, and 0 for the neutral and +1 states, confirming that the +3 channel has the highest time-averaged unitary conductance. Importantly, these relative $g_i$ values were obtained without a priori assumptions about whether a given charge state conducts or not. The same qualitative trend was observed by fitting the conductance of Weybridge M2, which yielded relative $g_i$ values of 0.47 \pm 0.07, 1.41 \pm 0.24, and 0.70 \pm 0.25 for the +2, +3, and +4 states, respectively (Figure S5a in the Supporting Information).

Both sets of proton current data indicate that the +2 state has nonvanishing proton fluxes that are 2–3-fold smaller than for the +3 state (Figure S5b). The time-averaged unitary conductance of the +4 channel has large uncertainties due to the difficulty of measuring whole-cell currents at the lowest pH.

**pH-Dependent Backbone Conformational Changes.** 2D $^{13}$C/$^{13}$C and $^{15}$N/$^{13}$C correlation spectra (Figure 3) revealed not only His37 side-chain structure but also backbone conformational changes as a function of pH. In general, the His37 Cz chemical shift increased and the C$\beta$ chemical shift decreased with decreasing pH, indicating that the His37 backbone became more helical. Four backbone conformations can be identified over the whole pH range. At pH 8.5, three nonideal helical conformations with distinct C$\alpha$, C$\beta$, and $^{15}$N chemical shifts were resolved (Figure 3d), whereas at low pH, the peaks were broadened and shifted to more ideal helical chemical shifts (Figure 3a). We designate these conformations as states 1–4, of which states 1–3 had been recently reported. These states do not correlate in a simple way to the charge states of the channel, since the M2TM conformation is also affected by the lipid membrane. At pH 5.2, the C$\alpha$–C$\beta$ cross-peaks indicate that the nonideal helical state 2 coexists with the broadly distributed ideal helical state 3 without fast exchange between them, since the two peaks appear at their limiting frequencies from 273 K (Figure 3b) to 308 K (Figure S3b in the Supporting Information). In view of the $^{13}$C chemical shift differences of \sim 300 Hz, any conformational exchange must be much slower than 300 s$^{-1}$. Decreasing the pH to 4.5 left only the broad peak for state 3, which has a shorter $^{15}$N $T_2$ than the other conformations (Table S1 in the Supporting Information), indicating that the low-pH peptide undergoes small-amplitude fluctuations and samples a broad conformational space. The fact that the average conformation of the low-pH peptide is more ideally helical suggests that the splayed-open packing of the C-terminal half of the helix in the low-pH crystal structure is present in bilayers, even though the crystal structure was determined using detergent-solubilized M2TM. Taken together, the 2D spectra indicate that multiple backbone conformations exist from pH 8.5 to 4.5 but that no fast interconversion occurs between the two main conformations at physiological acidic pH on the sub-10 ms time scale in the VM membrane.

**Figure 6.** $^{15}$N CP-MAS spectra of His37 in apo (a, c) and drug-bound (b, d) M2TM at (a, b) pH 5.2 and (c, d) pH 6.0 at 243, 273, and 308 K. Drug binding increased the unprotonated peak intensity at 250 ppm and reduced the exchange intensities.

**Figure 7.** 2D $^{15}$N–$^{13}$C correlation spectra of His37 and Gly34-labeled M2TM without and with Amt at 243 K. (a) pH 5.2 without drug. (b) pH 5.2 with Amt. (b) pH 8.5 without drug. Top row: backbone N–C$\alpha$ region. Bottom row: imidazole side-chain region. The drug-bound spectrum at pH 5.2 resembles the drug-free spectrum at pH 8.5.
Effects of Amt Binding on His37 Proton Exchange and Motion. If His37—water proton exchange is essential for proton conduction, then Amt binding should suppress this exchange and reestablish the $I_{\text{NH}}/I_{\text{NH}}$ ratios. Indeed, the $^{15}$N spectra of drug-bound M2TM at pH 6.0 and 5.2 (Figure 6) showed a significant increase in the 250 ppm intensity, suppression of the 213 ppm peak, and reduction in the 190–220 ppm intensity. 2D $^{15}$N–$^{13}$C correlation spectra confirmed that the drug-bound peptide at pH 5.2 has similar conformation as the apo peptide at pH 8.5 (Figure 7), indicating that Amt binding, although occurring at Ser31, inhibits $N_{\text{H}}$ protonation at His37. Recent water–protein $^1$H spin diffusion experiments showed that Amt binding dehydrated the N-terminal pore and reduced the water-exposed surface area of the protein by 2-fold. 12 Thus, inhibition of His37 protonation likely results from reduced accessibility to water. The effect of Amt on the $N_{\text{H}}$–$N_{\text{H}}$ exchange is weaker, as the 190–220 ppm intensity is partially retained (Figure 6b). This is consistent with the presence of water C-terminal to His37, as seen in both SSNMR data 23 and the 1.65 Å crystal structure. 16 When $N_{\text{H}}$ is unprotonated, $N_{\text{D}}$ must be protonated, giving the $\pi$ tautomer. Indeed, the 170 ppm peak of the $\pi$ tautomer is stronger in the drug-bound spectra than the apo spectra. The higher intensity of the 250 ppm peak (Figure 6b, d), which corresponds to a $pK_a$ reduction, is also consistent with previous results for DMPC/DMPG-bound M2TM. 43 Amt binding at pH 5.2 also perturbed the Gly34 conformation by shifting it to a less helical state, as seen in the 2D $^{15}$N–$^{13}$C correlation spectra (Figure 7b), indicating that the low-pH drug-complexed peptide adopts a conformation similar to the kinked helix of the apo peptide at high pH.

In the drug-free low-pH channel, the His37 side chain undergoes small-angle reorientations 23 that were proposed to orient the imidazole nitrogens to water molecules for proton transfer. To test whether this motion persists in the presence of the drug, we measured $C_{\text{OH}}–H$ dipolar couplings of the drug-bound M2TM at pH 5.2 and 6.0. Indeed, the $C_{\text{OH}}–H$ dipolar coupling reached the rigid limit at 308 K in the Amt-bound state, in contrast to the apo state at the same pH (Figure 8). Thus, the imidazolium ring motion is inhibited by Amt.

### DISCUSSION

These $^{15}$N NMR data, measured at physiological temperature, pH, and membrane composition, provide rich insights into the proton conduction mechanism of the influenza M2 channel. The imidazole nitrogens protonate and deprotonate at rates of $10^5$ s$^{-1}$, averaging the $^{15}$N isotropic chemical shifts. These rates were determined from CP-MAS spectra, which have rarely been used for quantitative kinetic analysis of systems undergoing chemical exchange because the analysis has been perceived as complex and difficult: in addition to the stochastic chemical exchange process, two separate coherent averaging processes are present, dipolar decoupling and magic-angle spinning, on time scales that are not sufficiently separate to make the problem easily reducible. Our novel analysis overcomes this difficulty and takes all these dynamic processes into account.

The 10$^5$ s$^{-1}$ proton exchange rate is about an order of magnitude larger than the proton transfer rates in buffered solutions, 3 indicating that His37 confinement in the water-filled pore speeds up the diffusion-limited proton transfer. The His37 proton exchange rate is consistent with the ring reorientation rate estimated from motional averaged dipolar couplings, 23 supporting the proposal that ring reorientation is synchronized with, and facilitates, proton transfer. The measured proton exchange rate is significantly higher than the time-averaged unitary proton flux of M2 from whole-cell patch-clamp and liposome experiments. 23, 44
This is expected because the NMR-detected exchange rate includes futile exchanges, where a proton may be transferred to and from His37 repeatedly without exiting the channel, which is likely due in part to the action of the gating residue Trp41.\textsuperscript{45,46} It should be noted that the reported open probabilities and unitary conductances of M2 vary widely because M2 is not a voltage- or ligand-gated channel and its conductance is too small to be measured accurately.

The His37 protonation and deprotonation require H-bonding with water: Amt binding in the N-terminal pore, which dehydrates the channel,\textsuperscript{42} completely suppressed the 213 ppm exchange peak (Figure 6b). In comparison, the Nε2 exchange intensity is partially retained in the presence of the drug, consistent with the retention of water C-terminal to His37.\textsuperscript{23} The water–His37 exchange agrees well with the observed water clusters above and below the His37 tetrad in the pH 6.5 crystal structure.\textsuperscript{16}

The absence of neutral–cationic histidine cross-peaks in the 2D spectra (Figure 3c) rules out the existence of strong H-bonds between histidines. In addition, the H-bonded dimer model requires the His37 χ3 angle to be 90°,\textsuperscript{15} which contradicts the χ3 angle of 180° measured in the lipid bilayer by SSNMR\textsuperscript{23} and in the detergent by crystallography.\textsuperscript{16} The 180° χ3 angle points Nα1 toward the N-terminus of the pore, supporting H-bonding with water rather than to a neighboring His.

The four pK\textsubscript{a}’s for the viral-membrane bound M2TM yielded the populations of the five charge states as a function of pH. Using these populations, we fit the proton conductances from two independent functional studies\textsuperscript{1,40} to obtain the relative conductances of the charge states. Both fits indicated that the +3 channel has the highest time-averaged unitary conductance and is thus chiefly responsible for M2’s proton channel activity (Figure 5c). The high g_{+3} can be due to a large open probability, a high intrinsic unitary conductance, or a combination of the two. Although the +2 channel has a lower g, its population is the largest in the physiological pH range, so it may be important for proton storage before full channel activation, as proposed recently.\textsuperscript{16} The +4 state has a smaller g than the +3 channel, even though it must have the highest open probability,\textsuperscript{46} suggesting that its intrinsic conductance g_{+4} is low. This is reasonable because the +4 tetrad exerts the largest repulsion with the proton, which should cause a higher energy barrier for proton transport than in the case of the +3 state, as predicted by calculations.\textsuperscript{20}

In the VM membrane, M2TM does not exhibit large-amplitude backbone conformational interconversion on the sub-10 ms time scale at physiological pH, contradicting the transporter model.\textsuperscript{25,26} Instead, we observed broad \textsuperscript{15}N line widths and short T2’s for the state that dominates at low pH (state 3), suggesting that the functionally relevant motions are small-amplitude fluctuations around a relatively ideal helical conformation. Although the VM membrane is relatively ordered because of the presence of cholesterol and sphingomyelin, the TM peptide retains its drug-binding ability in this membrane.\textsuperscript{47} Thus, the lack of large-scale transport-synchronized backbone motion cannot be attributed to the lack of conformational flexibility of the helical bundle. Instead, our data suggest a different type of protein backbone motion, entailing much smaller amplitudes, for proton transport.

**CONCLUSION**

In conclusion, these solid-state NMR data provide definitive evidence of His37 protonation and deprotonation at physiological acidic pH. The (1.0–4.5) × 10^{-5} s^{-1} proton transfer between His and water is synchronized with imidazole ring reorientations. The +3 channel has the highest time-averaged unitary conductance, defining the activated channel. We suggest that Trp41, through interactions with His37, reduces the high His37 proton exchange rate to the much smaller time-averaged proton flux. The lack of close contact between neutral and charged histidines rules out the H-bonded dimer model, while the lack of large-amplitude backbone conformational changes in the VM membrane modifies the transporter model. These findings support the shuttle mechanism, where protons from water molecules bind and unbind His37 on the microsecond time scale, facilitated by ring reorientation and small-amplitude backbone fluctuations.

**ASSOCIATED CONTENT**

Supporting Information. Additional equations for the correlation function, pK\textsubscript{a} analysis, tables of \textsuperscript{15}N T2 values, histidine intensity quantification, proton current data, and NMR spectra. This material is available free of charge via the Internet at http://pubs.acs.org.

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**REFERENCES**

Correlation function for two-site jumps

The correlation function for two-site exchange can be derived more stringently by considering \textit{a priori} probabilities $p_A = p_B = 0.5$ and conditional probabilities such as

\[ P_{AB}(\tau) = P_{BA}(\tau) = \left(1 - e^{-\tau/\tau_c}\right)/2 \] and \[ P_{AA}(\tau) = P_{BB}(\tau) = \left(1 + e^{-\tau/\tau_c}\right)/2 \] of moving from A to B within time $\tau$, so we can write

\[ C_\omega(\tau) \equiv \langle \omega(t)\omega(t + \tau) \rangle = \langle p_A\omega_AP_{AA}(\tau)\omega_A + p_A\omega_BP_{AB}(\tau)\omega_B + p_B\omega_BP_{BB}(\tau)\omega_B + p_B\omega_BP_{BA}(\tau)\omega_A \rangle \]

\[ = \langle \omega_A^2\left(1 + e^{-\tau/\tau_c}\right)/4 + \omega_A\omega_B\left(1 - e^{-\tau/\tau_c}\right)/2 + \omega_B^2\left(1 + e^{-\tau/\tau_c}\right)/4 \rangle \]

\[ = \left(\langle \omega_A^2 + \omega_B^2 \rangle\left(1 + e^{-\tau/\tau_c}\right)/4 + \langle \omega_A\omega_B \rangle \left(1 - e^{-\tau/\tau_c}\right)/2 \right) \]

\[ = \left(\langle \omega_A^2 - \omega_B^2 \rangle/4 \right) e^{-\tau/\tau_c} + \left(\langle \omega_A + \omega_B \rangle^2/4 \right) \]

Thus, at $\tau = \infty$, \[ C_\omega(\infty) = \left(\langle \omega_A + \omega_B \rangle/2 \right)^2. \]

Analysis of proton dissociation constants

We extracted the proton dissociation constants \cite{1} by considering the four equilibrium reactions:
where the four proton dissociation constants are:

\[
\begin{align*}
K_{a1} &= \frac{[\text{His}_4 H_3^{3+}] [H^+]}{[\text{His}_4 H_4^{2+}]}, \\
K_{a2} &= \frac{[\text{His}_4 H_2^{2+}] [H^+]}{[\text{His}_4 H_3^{3+}]}, \\
K_{a3} &= \frac{[\text{His}_4 H_1^+] [H^+]}{[\text{His}_4 H_2^{2+}]}, \\
K_{a4} &= \frac{[\text{His}_4] [H^+]}{[\text{His}_4 H_1^+]},
\end{align*}
\]

(S3)

By integrating the unprotonated and protonated \(^{15}\text{N}\) peaks, we obtain the ratio of neutral to cationic His:

\[
\frac{[\text{His}]}{[\text{His}^H]} = \frac{I_N \cdot \kappa}{(I_{NH} - I_N \cdot \kappa)/2} = \frac{2}{(I_{NH}/I_N)/\kappa - 1},
\]

(S4)

where \(\kappa\) is a scaling factor to account for the different CP efficiencies between the N and NH peaks.

Based on equations (2-4), the \([\text{His}]/[\text{His}^H]\) ratio depends on the \(pK_a\)'s according to:

\[
\begin{align*}
\frac{[\text{His}]}{[\text{His}^H]} = & \frac{1 \cdot [\text{His}_4 H_3^{3+}] + 2 \cdot [\text{His}_4 H_2^{2+}] + 3 \cdot [\text{His}_4 H_1^+] + 4 \cdot [\text{His}_4]}{4 \cdot [\text{His}_4 H_4^{2+}] + 3 \cdot [\text{His}_4 H_3^{3+}] + 2 \cdot [\text{His}_4 H_2^{2+}] + 1 \cdot [\text{His}_4 H_1^+]}, \\
= & \frac{1 \cdot K_{a1} \cdot 10^{-pH} + 2 \cdot K_{a1} \cdot K_{a2} \cdot 10^{-2pH} + 3 \cdot K_{a1} \cdot K_{a2} \cdot K_{a3} \cdot 10^{-3pH} + 4 \cdot K_{a1} \cdot K_{a2} \cdot K_{a3} \cdot K_{a4} \cdot 10^{-4pH}}{4 \cdot 3 \cdot K_{a1} \cdot 10^{-pH} + 2 \cdot K_{a1} \cdot K_{a2} \cdot 10^{-2pH} + 1 \cdot K_{a1} \cdot K_{a2} \cdot K_{a3} \cdot 10^{-3pH}}.
\end{align*}
\]

(S5)

Fitting the pH-dependent \([\text{His}]/[\text{His}^H]\) thus yields the four \(pK_a\)'s.

The integrated intensities of protonated and unprotonated \(^{15}\text{N}\) peaks were taken from the 243 K \(^{15}\text{N}\) spectra. For the unprotonated \(^{15}\text{N}\) site, the centerband (~250 ppm) and sideband intensities were added. For the protonated \(^{15}\text{N}\) site, intensities in the 150 - 200 ppm range were integrated. All spectra
were measured at the same magnetic field strength (9.4 Tesla) and MAS rate to ensure comparable experimental efficiencies for different samples. The CP efficiency factor $\kappa$ was measured from the $^{15}$N spectrum of neutral histidine (Fig. S4) using the same conditions as for the membrane samples. With a CP contact time of 3 ms, after maximizing the unprotonated $^{15}$N peak, the unprotonated $^{15}$N intensity is 1.464 times lower than the protonated intensity. Thus, $\kappa = 1.464$ was used to multiply the unprotonated $^{15}$N intensities of all M2TM spectra to obtain the correct $I_{NH}/I_N$. Intensity error bars were estimated based on the signal-to-noise ratios of the spectra and propagated to the error bars for the $[\text{His}]/[\text{HisH}^+]$ ratios.
Table S1. M2TM $^{15}$N $T_2$ (ms) and intrinsic linewidths (Hz) at 308 K as a function of pH.

<table>
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<th>$^{15}$N $T_2$ (ms)</th>
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</tr>
<tr>
<td>Broad peak</td>
<td>190-220</td>
<td>-</td>
<td>0.8 ms</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>400 Hz</td>
</tr>
</tbody>
</table>
Table S2. $^{15}$N intensities and the neutral to charged histidine ratios as a function of pH.

<table>
<thead>
<tr>
<th>pH</th>
<th>$I_{NH}/I_N$</th>
<th>$[\text{His}]/[\text{HisH}^+]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.5</td>
<td>11.3±1.0</td>
<td>0.30±0.08</td>
</tr>
<tr>
<td>5.2</td>
<td>5.4±0.5</td>
<td>0.74±0.15</td>
</tr>
<tr>
<td>6.0</td>
<td>4.5±0.3</td>
<td>0.96±0.14</td>
</tr>
<tr>
<td>7.0</td>
<td>2.75±0.10</td>
<td>2.28±0.17</td>
</tr>
<tr>
<td>8.5</td>
<td>1.55±0.04</td>
<td>34.1±3.8</td>
</tr>
</tbody>
</table>

Table S3. Measured proton currents of Udorn M2 and chord conductance of Weybridge M2.

<table>
<thead>
<tr>
<th>pH&lt;sub&gt;out&lt;/sub&gt;</th>
<th>$I/I_{\text{max}}$, Udorn</th>
<th>$V-E_H$ (V), Udorn</th>
<th>$g/g_{\text{max}}$, Udorn</th>
<th>$g/g_{\text{max}}$, Weybridge</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.0</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1</td>
</tr>
<tr>
<td>4.2</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>0.98±0.08</td>
</tr>
<tr>
<td>4.5</td>
<td>1</td>
<td>-0.293</td>
<td>1.00</td>
<td>0.95±0.05</td>
</tr>
<tr>
<td>5.0</td>
<td>0.855</td>
<td>-0.264</td>
<td>0.950</td>
<td>0.86±0.06</td>
</tr>
<tr>
<td>5.5</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>0.80±0.06</td>
</tr>
<tr>
<td>5.8</td>
<td>0.511</td>
<td>-0.217</td>
<td>0.691</td>
<td>0.60±0.11</td>
</tr>
<tr>
<td>6.0</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>0.48±0.10</td>
</tr>
<tr>
<td>6.2</td>
<td>0.267</td>
<td>-0.195</td>
<td>0.402</td>
<td>0.29±0.06</td>
</tr>
<tr>
<td>6.5</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>0.18±0.04</td>
</tr>
<tr>
<td>6.8</td>
<td>0.137</td>
<td>-0.159</td>
<td>0.253</td>
<td>-</td>
</tr>
<tr>
<td>7.2</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>0.10±0.02</td>
</tr>
<tr>
<td>7.5</td>
<td>0.0382</td>
<td>-0.120</td>
<td>0.0934</td>
<td>-</td>
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<tr>
<td>8.2</td>
<td>0.0153</td>
<td>-0.080</td>
<td>0.0561</td>
<td>-</td>
</tr>
</tbody>
</table>

<sup>a</sup> The A/Udorn/72 M2 proton currents were measured at $pH_{in}$ = 7.5, V = -120 mV and T = 290 K, and the Weybridge M2 conductance was measured at $pH_{in}$ = 7.4 and an applied voltage of -60 mV.
Fig. S1. Aromatic region of the $^{13}$C CP-MAS spectra of His37-labeled M2TM in a virus-mimetic membrane. (a) Spectra as a function of pH at 273 K. (b) Spectra of the pH 5.2 sample as a function of temperature. Asterisks denote MAS sidebands. The Cδ2 and Cγ peaks are good indicators of the histidine charge state. The Cδ2 peak moves from 113.1 to 117.6 ppm upon Nδ1 protonation, while the Cγ peak moves from 135.5 to 128.8 ppm. As the pH decreases, the cationic (green) Cδ2 and Cγ intensities increase while the neutral (red) Cδ2 peak intensity decreases.
Fig. S2. $^{15}$N $T_2$ relaxation of M2TM at 308 K as a function of pH. (a) pH 5.2. (b) pH 6.0. (c) pH 8.5. The spectra were measured using a Hahn-echo pulse sequence with a $^1$H decoupling field strength of 62.5 kHz. Representative spectra are shown in the bottom row. Black spectra were measured with no echo delay while red spectra were measured with an echo delay. The broad 190-220 ppm peak has moderately shorter $T_2$ than the other sidechain signals. The backbone amides have much longer $T_2$’s than the sidechain nitrogens.
Fig. S3. 2D $^{13}$C-$^{13}$C correlation spectra of His37-labeled M2TM in VM membranes to test the hydrogen-bonded dimer model and the transporter model. (a) Aromatic region of the 2D spectrum of the pH 6 sample, measured with a 300 ms mixing time at 273 K. No neutral-cationic $^\delta_2(\tau)$ – $^\delta_2(+)$ cross peak was observed (yellow shade), even though both species exist at this pH. (b) His37 backbone region of the 2D spectrum of the pH 5.2 sample at 273 K and 308 K. No chemical shift averaging is present at high temperature, indicating the lack of fast exchange between the less helical, non-conducting conformation and the more helical, conducting conformation.
Fig. S4. $^{15}$N CP-MAS spectrum of U-$^{13}$C, $^{15}$N-labeled His at pH 8.5 to determine the CP scaling factor $\kappa$ between unprotonated and protonated $^{15}$N. The $^1$H-$^{15}$N CP contact time was 3 ms and the CP matching conditions were optimized in the same way as for membrane-bound M2TM. The integrated intensity of the unprotonated $N_\delta$1 is 1.464 less than the $Ne_2$H intensity, even though the two nitrogens are equimolar. This scaling factor was applied in calculating the neutral to cationic His ratio in M2TM.
**Fig. S5.** Fitting the M2 proton conductance and current using the His37 pKₐ’s. (a) Best fit of the conductance data of Chizhmakov et al (squares) of Weybridge M2, giving relative time-averaged conductance of 0.47 : 1.41 : 0.70 for the +2, +3 and +4 channels. (b) Proton currents (squares) of Udorn M2 at an applied voltage of -120 mV and a pH in of 7.5. Solid lines represent best-effort fit obtained assuming zero conductance by the +2 channel. The +3 and +4 currents are adjusted relative to each other, but do not give satisfactory fit to the currents. Thus, the +2 state cannot have zero conductance.

**References**

